

Preface

This book is about calculations on the thermodynamics of biochemical reactions that is based on Legendre transforms of the Gibbs energy that bring in the pH, pMg, and concentrations of coenzymes and ligands as independent variables. Chemical reactions are studied under the constraints of constant temperature and constant pressure, but biochemical reactions are studied under the additional constraints of pH and, perhaps, pMg or free concentrations of other metal ions. In considering systems of biochemical reactions, it may be useful to constrain concentrations of various coenzymes. In considering macromolecule-ligand binding it may be useful to constrain the ligand concentration. For example, the binding of oxygen by hemoglobin can be treated at specified concentrations of molecular oxygen. As more intensive variables are specified, more thermodynamic properties of a system are defined, and the equations that represent thermodynamic properties as functions of independent variables become more complicated. Since more independent variables are involved in biochemical thermodynamics than in chemical thermodynamics, the equations for calculating properties become more complicated. Thanks to the development of mathematical applications for personal computers, these complicated calculations can be carried out much more easily. Thermodynamic calculations on such systems require the use of computers, and *Mathematica* is a very convenient application because of its symbolic capabilities, its calculation of partial derivatives, and its facilities for construction of databases, tables, and plots. The fact that *Mathematica* can be used to derive these very complicated functions and take partial derivatives to obtain other properties makes it possible to make calculations that would previously have been considered impractical. Therefore, this book has been written in *Mathematica*. *Mathematica* makes it possible to intermingle text with calculations, as illustrated by a number of recent books. In this book, the calculations of biochemical thermodynamics are described in words, equations are derived by use of *Mathematica*, and then evaluated for specified values of independent variables. All the *Mathematica* calculations are shown, and so the data, equations and programs can be used for the calculation of properties of reactants at other specified values of independent variables.

The main question that thermodynamics deals with is the direction of spontaneous change when a system is initially in a specified state. The state of a biochemical reaction system is described by specifying concentrations of reactants, temperature, pH, ionic strength, and concentrations of free metal ions that are bound by reactants. Concentrations of coenzymes and ligands like molecular oxygen can also be specified. Thermodynamics is important in biochemistry because it can tell us whether a given enzyme-catalyzed reaction or ligand binding will go to the right or to the left under specified conditions. It can also give us the equilibrium composition. Enzymes determine the reactions that are catalyzed in a given system and their rates, but enzymes do not determine the directions of reactions or the amount of energy that is stored, transferred, or is required to synthesize a needed reactant. In a cell, certain reactions are needed to store energy and other reactions are needed to use this energy for necessary purposes of life. If we want to understand how energy is stored and used, we need to know the apparent equilibrium constants K' of the reactions involved under the ambient conditions and also heats of reaction. Other biochemical reactions, like the binding of oxygen by hemoglobin do not require enzyme catalysis, but the equilibrium extents of binding reactions and the influence of other ligands are determined by thermodynamics. With knowledge of pKs, a measurement of the apparent equilibrium constant K' of a biochemical reaction at a single pH and ionic strength makes it

possible to calculate K' as a function of pH and ionic strength. When enthalpies of reaction are available and enthalpies of acid dissociation are known, a measurement of K' at a single temperature, pH, and ionic strength makes it possible to calculate K' and other transformed thermodynamic properties as functions of temperature, pH, and ionic strength.

The apparent equilibrium constants of about 500 enzyme-catalyzed reactions have been determined under various sets of conditions, and enthalpy changes have been measured calorimetrically for some of these reactions or can be calculated from the effect of temperature on the apparent equilibrium constant. In principle these data can be used to calculate standard Gibbs energies of formation and standard enthalpies of formation for the species of about 1000 reactants. The current number of known species matrices is 199. For 94 of these reactants, the $\Delta_f H^\circ$ of all species are known. Further analysis of existing experimental data and new measurements will make it possible to extend the current database BasicBiochemData3. The most efficient way to store thermodynamic information on enzyme-catalyzed reactions is to store data on species because then apparent equilibrium constants and other transformed thermodynamic properties of reactants and reactions can be calculated for specified conditions. Such a database makes it possible to calculate apparent equilibrium constants and transformed thermodynamic properties for many more reactions than it takes to make the data table. An even larger data set can be based on analogies because of similarities in the underlying chemistry of some reactions. Such a database can be used to calculate apparent equilibrium constants that are too large to measure directly. The number of apparent equilibrium constants that can be calculated from a database increases exponentially with the number of reactants in the data base. The calculation of species properties from different enzyme-catalyzed reactions reveals inconsistencies between different equilibrium and calorimetric experiments.

Apparent equilibrium constants cannot be determined experimentally on reactions that go nearly completion. Calorimetric measurements of enthalpies of reaction do not have this problem. Proteins may be reactants in enzyme-catalyzed reactions. When apparent equilibrium constants can be measured on reactions involving proteins, the thermodynamic properties of the reaction site in the protein can be calculated.

It is assumed that the reader has had some introduction to thermodynamics at the level of an undergraduate course in physical chemistry. My previous book "Thermodynamics of Biochemical Reactions," Wiley, Hoboken, NJ (2003) provides a more complete introduction to the structure of thermodynamics and its relation to statistical mechanics. This successor book is needed because more recent research has clarified the structure of biochemical thermodynamics and opened up new possibilities for learning about the flow of energy in living things. Three aspects of these calculations are as follows:

1. Experimental data on enzyme-catalyzed reactions are in the form of apparent equilibrium constants K' , heats of reaction, and pKs (and corresponding heats of dissociation), but the most efficient way to store the thermodynamic properties of biochemical reactions is by means of small matrices that give standard Gibbs energies of formation, standard enthalpies of formation, charge numbers, and numbers of hydrogen atoms in each species of a reactant. The bridge between treating enzyme-catalyzed reactions in terms of species and in terms of reactants, like ATP, which is a sum of species, is provided by the Legendre transform $G' = G - n_c(H) \mu(H^+)$, where G' is the transformed Gibbs energy of the system, G is the Gibbs energy of the system, $n_c(H)$ is the amount of the hydrogen component in the system (total amount of hydrogen atoms), and $\mu(H^+)$ is the specified chemical potential of hydrogen ions, which is determined by the pH. The standard transformed Gibbs energy of a biochemical reaction is given by $\Delta_r G'^\circ = -RT \ln K'$. The dependence of thermodynamic properties on ionic strength can be calculated using the extended Debye-Hückel equation, which involves a temperature-dependent parameter. When a reactant consists of pseudoisomers that are at equilibrium at a specified pH, isomer group thermodynamics has to be used to calculate the standard transformed Gibbs energy of formation $\Delta_f G'^\circ$ of the reactant. This process leads to functions of temperature, pH, and ionic strength that are too complicated to be written out by hand, but *Mathematica* can be used to derive these functions and to calculate the standard transformed enthalpy of formation, standard transformed entropy of formation, average number of hydrogen ions bound, and other thermodynamic properties by taking partial derivatives.
2. Going from the experimental thermodynamic properties K' and transformed enthalpies of reaction to properties of species involves the concept of the inverse Legendre transform ($G = G' + n_c(H) \mu(H^+)$). Computer programs can be written to go from the experimental properties directly to the standard Gibbs energies of formation and standard enthalpies of formation of the species involved in a reactant. These programs are more complicated than the programs using properties of species to derive the standard transformed thermodynamic properties of reactants.

3. Equilibrium compositions of systems of chemical reactions or systems of enzyme-catalyzed reactions can only be calculated by iterative methods, like the Newton-Raphson method, and so computer programs are required. These computer programs involve matrix operations for going back and forth between conservation matrices and stoichiometric number matrices. A more global view of biochemical equilibria can be obtained by specifying steady-state concentrations of coenzymes. These are referred to as calculations at the third level to distinguish them from the first level (chemical thermodynamic calculations in terms of species) and the second level (biochemical thermodynamic calculations at specified pH in terms of reactants).

In *Mathematica* reactants need to be named with words starting with lower case letters because words starting with capital letters refer to operations. Also the names of reactants need to be as short as convenient and cannot involve spaces, subscripts, superscripts, hyphens, dots or other symbols that are *Mathematica* operations. Therefore, ATP is referred to as *atp* both in the text and in computer programs. Most of these abbreviated names will be recognized immediately, but a glossary of names is provided in the Appendix.

The Appendix contains a copy of the *Mathematica* notebook BasicBiochemData3.nb, Tables of Transformed Thermodynamic Properties, the Glossary of Names of Reactants, the Glossary of Symbols for Thermodynamic Properties, a List of *Mathematica* programs, and Sources of Biochemical Thermodynamic Information on the Web. The *Mathematica* package BasicBiochemData3.m, which is also available at

<http://library.wolfram.com/infocenter/MathSource/5704>

contains all of the species data at 298.15 K and zero ionic strength. It also contains functions of pH and ionic strength for the standard transformed Gibbs energies of formation of 199 reactants at 298.15 K; these functions are named *atp*, *adp*,... The functions are also given for the average number of hydrogen atoms in the reactant at 298.15 K as functions of the pH and ionic strength; these functions are named *atpNH*, *adpNH*,... Since $\Delta_f H^\circ$ values are known for all species of 94 reactants at 298.15 K and zero ionic strength, the functions of temperature, pH, and ionic strength are given for these 94 reactants for the following transformed thermodynamic properties: $\Delta_f G'^\circ$ (named *atpGT*, *adpGT*,...), $\Delta_f H'^\circ$ (named *atpHT*, *adpHT*,...), $\Delta_f S'^\circ$ (named *atpST*, *adpST*,...), and $\bar{N}_H$ (named *atpNHT*, *adpNHT*,...).

Since functions of pH and ionic strength for $\Delta_f G'^\circ$ and $\bar{N}_H$ are known for 199 reactants at 298.15 K, $\Delta_f G'^\circ$ and $\Delta_f \bar{N}_H$ are calculated in Chapter 12 for 229 enzyme-catalyzed reactions as functions of pH and ionic strength. Since $\Delta_f G'^\circ$ and $\Delta_f H'^\circ$ are known for all the species of 94 reactants, functions of temperature, pH, and ionic strength that yield $\Delta_f G'^\circ$, $\Delta_f H'^\circ$, $\Delta_f S'^\circ$, and $\bar{N}_H$ for 90 enzyme-catalyzed reactions are given in Chapter 13.

It is not necessary to be a programmer in order to use the programs and procedures illustrated in this book. Names of reactants, temperatures, pHs, and ionic strengths are readily changed in using the various programs.

The CD at the back of the book contains the whole book in *Mathematica*. It can be downloaded into a personal computer with *Mathematica* installed, but it can be read on a computer with *MathReader*, which is freely available from Wolfram Research, Inc. (100 Trade Center Drive, Champaign, IL 61820-7237, and www.wolfram.com). A chapter can be downloaded into a personal computer as a notebook. The following chapters do not require that BasicBiochemData3 be loaded: Chapters 2, 3, 5, 6, and 14. Chapters 1, 4, 7, 8, 9, 10, 11, 12, 13, and 15 need BasicBiochemData3 to be loaded by typing <<BiochemThermo`BasicBiochemData3` (see Use of *Mathematica*).

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